-22AIE203-  
Data structures and algorithms -2

**Name: Girish S Roll No.: AM.EN.U4AIE22044**

# ASSIGNMENT 5 – Sparse Matrix and Block Matrix

--------------------------------------------------------------------------



Sparse Matrix

class SparseMatrix:

     def \_\_init\_\_(self, rows, cols):

*self*.\_\_data = [[rows, cols, 0]]

     def \_\_setitem\_\_(self, key, value):

          if (key[0] > *self*.\_\_data[0][0]-1) or (key[1] > *self*.\_\_data[0][1]-1):

               print(f"Invalid Indexing: {key} for size of {tuple(*self*.\_\_data[0][:2])}")

          if *self*[key] == 0:

*self*.\_\_data[0][2]+=1

*self*.\_\_data.append([key[0], key[1], value])

               header = *self*.\_\_data[0]

               data = sorted(*self*.\_\_data[1:])

*self*.\_\_data = [header]

               for i in data:

*self*.\_\_data.append(i)

          else:

               header = *self*.\_\_data[0]

*self*.\_\_data = [[i[0], i[1], value] if tuple(i[:2]) == key else i for i in *self*.\_\_data[1:]]

*self*.\_\_data.insert(0, header)

     def \_\_getitem\_\_(self, key):

          if (key[0] > *self*.\_\_data[0][0]-1) or (key[1] > *self*.\_\_data[0][1]-1):

               print(f"Invalid Indexing: {key} for size of {(*self*.\_\_data[0][0]-1, *self*.\_\_data[0][1]-1)}")

               return None

          for i in *self*.\_\_data[1:]:

               if (i[0], i[1]) == key:

                    return i[2]

          return 0

     def \_\_add\_\_(self, other):

          if *self*.\_\_data[0][:2] == other.\_\_data[0][:2]:

               header = *self*.\_\_data[0]

               newinstance = SparseMatrix(header[0], header[1])

               for i in *self*.\_\_data[1:]:

                    newinstance[(i[0], i[1])] = i[2]

               for i in other.\_\_data[1:]:

                    newinstance[(i[0], i[1])] = newinstance[(i[0], i[1])] + i[2]

               return newinstance

          else:

               print(f"Dimension Error: the Dimensions ({*self*.\_\_data[0][0]}, {*self*.\_\_data[0][1]}) and ({other.\_\_data[0][0]}, {other.\_\_data[0][1]}) doesn't match")

     def \_\_str\_\_(self):

          res=""

          data = [[0 for i in range(*self*.\_\_data[0][1])] for i in range(*self*.\_\_data[0][0])]         *#[[0]\*self.\_\_data[0][1]]\*self.\_\_data[0][0]*

          for i in *self*.\_\_data[1:]:

               data[i[0]][i[1]] = i[2]

          for i in data:

               for j in i:

                    res+="{:>5}".format(round(j, 2))

               res+="\n"

          return res[:-1]

     def display(self):

          print("+-----+-----+-----+-----+")

          print("| Ind | Row | Col | Val |")

          print("+-----+-----+-----+-----+")

          for i, val in enumerate(*self*.\_\_data):

               if i==0:

                    print("| {:<3} | {:<3} | {:<3} | {:<3} |".format(i+1, val[0], val[1], val[2]))

                    print("+-----+-----+-----+-----+")

                    continue

               print("| {:<3} | {:<3} | {:<3} | {:<3} |".format(i+1, val[0]+1, val[1]+1, val[2]))

          print("+-----+-----+-----+-----+")

     def transpose(self):

          for i in *self*.\_\_data:

               i[0], i[1] = i[1], i[0]

     def inverse(self):

          if *self*.\_\_data[0][0] != *self*.\_\_data[0][1]:

               print("Inverse Error: The Matrix is not a square matrix")

               return

          if *self*.determinant() == 0:

               print("Inverse Error: The Matrix is Indefinite Matrix")

               return

          matrix = [[0 for \_ in range(*self*.\_\_data[0][1])] for \_ in range(*self*.\_\_data[0][0])]

          for i in *self*.\_\_data[1:]:

               matrix[i[0]][i[1]] = i[2]

          n = len(matrix)

          identity = [[0] \* n for \_ in range(n)]

          for i in range(n):

             identity[i][i] = 1

*# Gaussian Inverse*

          for i in range(n):

*# Partial pivoting*

               max\_row = i

               for j in range(i + 1, n):

                    if abs(matrix[j][i]) > abs(matrix[max\_row][i]):

                         max\_row = j

               matrix[i], matrix[max\_row] = matrix[max\_row], matrix[i]

               identity[i], identity[max\_row] = identity[max\_row], identity[i]

               scalar = 1.0 / matrix[i][i]

               for j in range(n):

                    matrix[i][j] \*= scalar

                    identity[i][j] \*= scalar

               for j in range(n):

                    if i != j:

                         scalar = matrix[j][i]

                         for k in range(n):

                              matrix[j][k] -= scalar \* matrix[i][k]

                              identity[j][k] -= scalar \* identity[i][k]

*self*.\_\_data = [*self*.\_\_data[0]]

*self*.\_\_data[0][2] = 0

          for i in range(*self*.\_\_data[0][0]):

               for j in range(*self*.\_\_data[0][1]):

                    if identity[i][j] != 0:

*self*[(i, j)] = identity[i][j]

     def determinant(self):

          if *self*.\_\_data[0][0] != *self*.\_\_data[0][1]:

               print("Determinant Error: The matrix is not square")

               return None

          matrix = [[0 for \_ in range(*self*.\_\_data[0][1])] for \_ in range(*self*.\_\_data[0][0])]

          for i in *self*.\_\_data[1:]:

               matrix[i[0]][i[1]] = i[2]

          det = 1

          for i in range(*self*.\_\_data[0][0]):

               maxElem = abs(matrix[i][i])

               maxRow = i

               for k in range(i + 1, *self*.\_\_data[0][0]):

                    if abs(matrix[k][i]) > maxElem:

                         maxElem = abs(matrix[k][i])

                         maxRow = k

               if i != maxRow:

                    det \*= -1

                    matrix[i], matrix[maxRow] = matrix[maxRow], matrix[i]

               det \*= matrix[i][i]

               if matrix[i][i] == 0:

                    return 0  *# Determinant is 0 if diagonal element becomes 0*

               for k in range(i + 1, *self*.\_\_data[0][0]):

                    c = 0

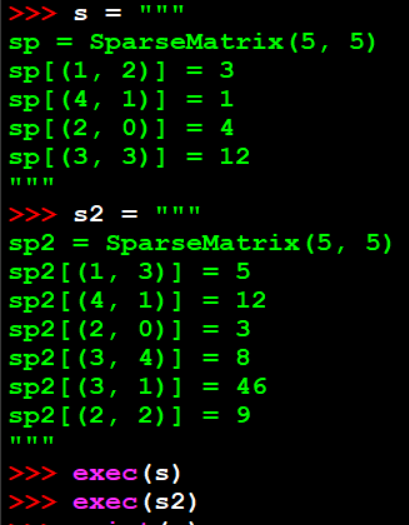
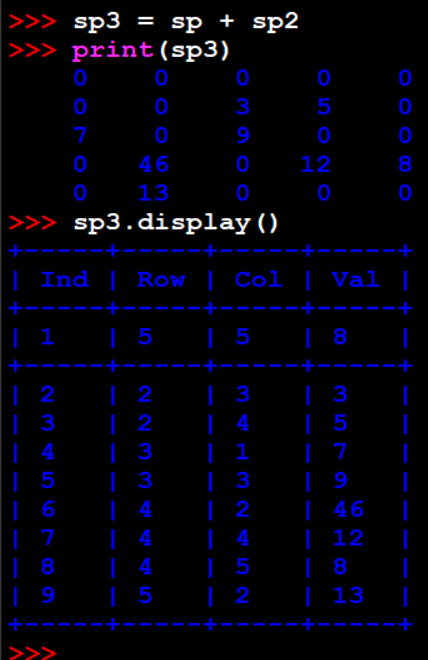
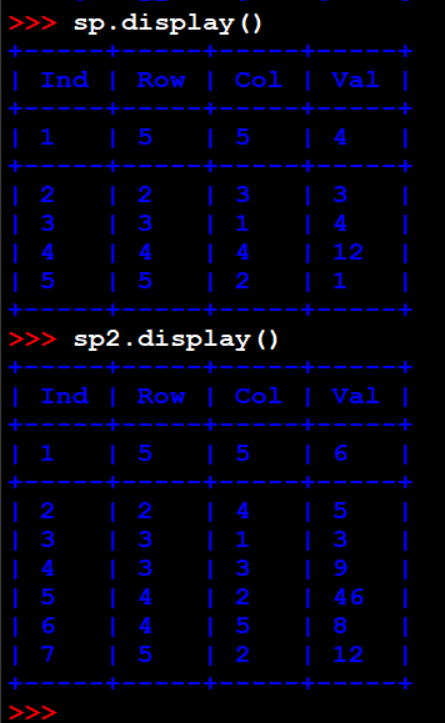
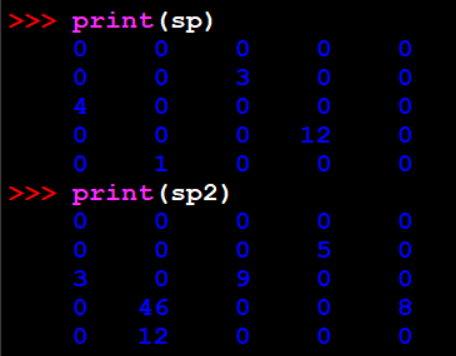
                    if matrix[k][i] != 0:

                         c = -matrix[k][i] / matrix[i][i]

                         for j in range(i, *self*.\_\_data[0][0]):

                              matrix[k][j] += c \* matrix[i][j]

          return det

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Block Matrix

class BlockMatrix:

    def \_\_init\_\_(self, size, block\_size):

*self*.size = size

*self*.block\_size = block\_size

*self*.num\_blocks = size // block\_size

*self*.blocks = [[[0] \* block\_size for \_ in range(block\_size)] for \_ in range(*self*.num\_blocks \*\* 2)]

    def insert(self, row, col, value):

        block\_row = row // *self*.block\_size

        block\_col = col // *self*.block\_size

        inner\_row = row % *self*.block\_size

        inner\_col = col % *self*.block\_size

*self*.blocks[block\_row \* *self*.num\_blocks + block\_col][inner\_row][inner\_col] = value

    def display(self):

        for i in range(*self*.num\_blocks):

            for j in range(*self*.num\_blocks):

                print("Block ({}, {}):".format(i, j))

                for row in range(*self*.block\_size):

                    for col in range(*self*.block\_size):

                        global\_row = i \* *self*.block\_size + row

                        global\_col = j \* *self*.block\_size + col

                        if global\_row < *self*.size and global\_col < *self*.size:

                            print(*self*.blocks[i \* *self*.num\_blocks + j][row][col], end=" ")

                        else:

                            print("0", end=" ")

                    print()

                print()

def conformal\_decomposition(matrix):

     length = len(matrix)

     if length != len(matrix[0]):

          print(f"Invalid Dimension Error: Expected a square matrix but a Matrix({length}x{len(matrix[0])}) was given.")

          return None, None

     diamat = [[0]\*length for i in range(length)]

     offdiamat = [[0]\*length for i in range(length)]

     for i in range(length):

          for j in range(length):

               if i == j:

                    diamat[i][j] = matrix[i][j]

               else:

                    offdiamat[i][j] = matrix[i][j]

     return diamat, offdiamat

matrix = BlockMatrix(4, 2)

value = 1

for i in range(4):

    for j in range(4):

        matrix.insert(i, j, value)

        value += 1

print("Block Matrix:")

matrix.display()

mat = [[1, 2, 3], [4, 5, 6], [7, 8, 9]]

print("Conformal Decomposition matrix:")

for i in mat:

     for j in i:

          print("{:>5}".format(j), end="")

     print()

diamat, offdiamat = conformal\_decomposition(mat)

print("Diagonal Matrix: ")

for i in diamat:

     for j in i:

          print("{:>5}".format(j), end="")

     print()

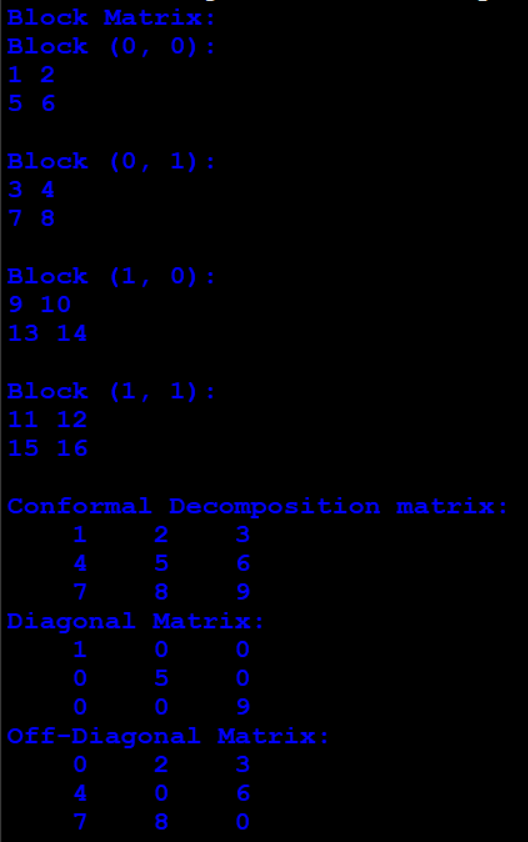
print("Off-Diagonal Matrix: ")

for i in offdiamat:

     for j in i:

          print("{:>5}".format(j), end="")

     print()

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